ÉCOLE POLYTECHNIQUE
FÉDÉRALE DE LAUSANNE

Disal

Lab 5

Signals, Instruments and Systems

School of Architecture, Civil and Environmental Engineering

http://disal.epfl.ch/teaching/signals_instruments_systems/

Meeting room

Tutorial: https://epfl.zoom.us/j/902099047

Q&A: https://epfl.zoom.us/j/185667699

- You will first be in a “waiting room” before the TA lets you in
- You will be assigned to one of the “breakout rooms” where a TA will answer your questions one on one.
- The breakout room assignment will be done by us, you don’t need to do anything.

Lab 5 Outline

- Concepts:
  - Convolution
  - Sampling
  - Aliasing
  - Reconstruction
- Tools:
  - Matlab

Part 1: Continuous Convolution

$$(f * g)(t) = \int_{-\infty}^{\infty} f(\tau) \cdot g(t-\tau) d\tau$$

- For each value of *t*:
  1. Flip (reflect) ***g***
  2. Shift ***g*** by ***t***
  3. Multiply ***f*** and ***g***
  4. Integrate over $\boldsymbol{\tau}$

1) $g(\tau) \rightarrow g(-\tau)$

2) $g(-\tau) \rightarrow g(t-\tau)$

3) $f(\tau) \cdot g(t-\tau)$

4) $\int_{-\infty}^{\infty} f(\tau) \cdot g(t-\tau) d\tau$

- Note that the result does **not** depend on τ!

Part 2: Discrete Convolution

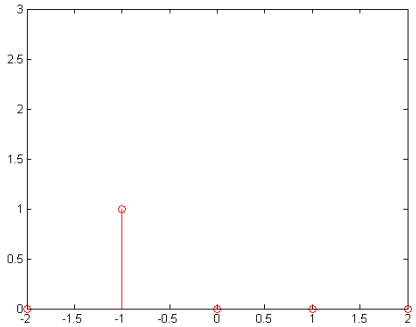
$$(f * g)(t) = \int_{-\infty}^{\infty} f(\tau) \cdot g(t-\tau) d\tau$$

$$\downarrow$$

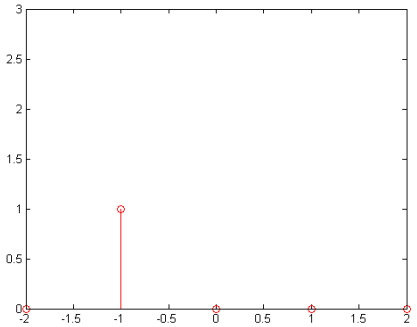
$$(f * g)(n) = \sum_{m=-\infty}^{\infty} f(m) \cdot g(n-m)$$

- Similar to the continuous version
- The integral becomes an infinite sum
- Matlab, operating on a computer, can only emulate continuity and therefore use the discrete version with an adjustable discretization level in time and amplitude

Example of Discrete Convolution



f[m]



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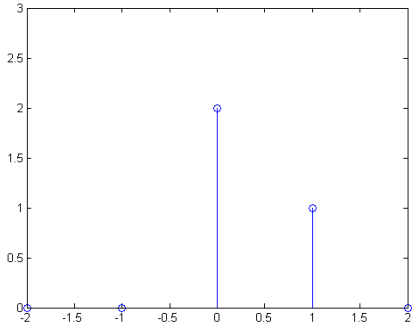
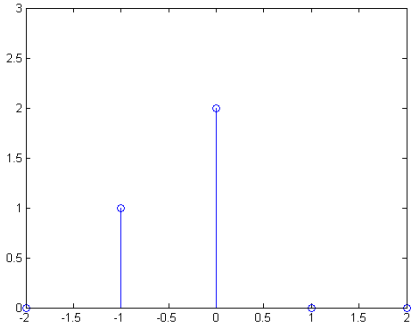


g[m]



g[-m]

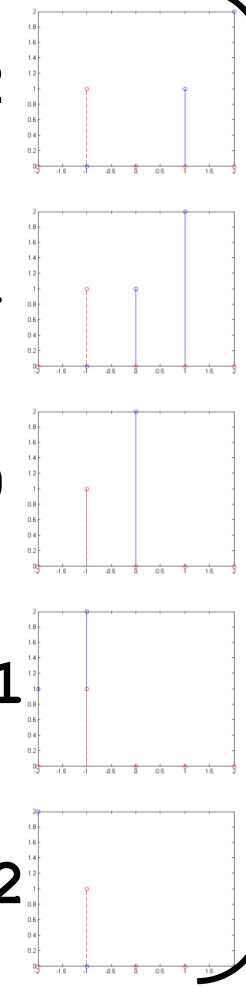
n=2

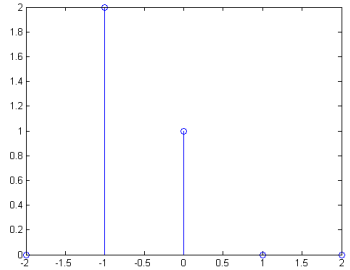
n=1

n=0

n=-1

n=-2





(f*g)[n]

Part 3: Sampling and reconstruction

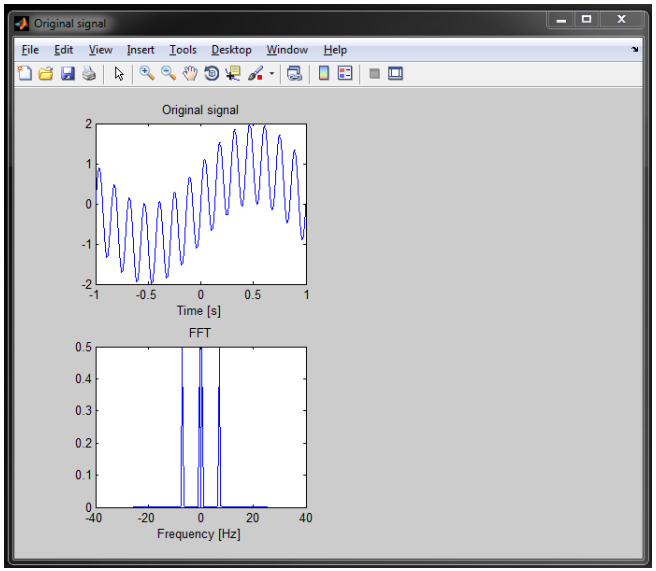
Signal generation → Filtering → Sampling → Reconstruction

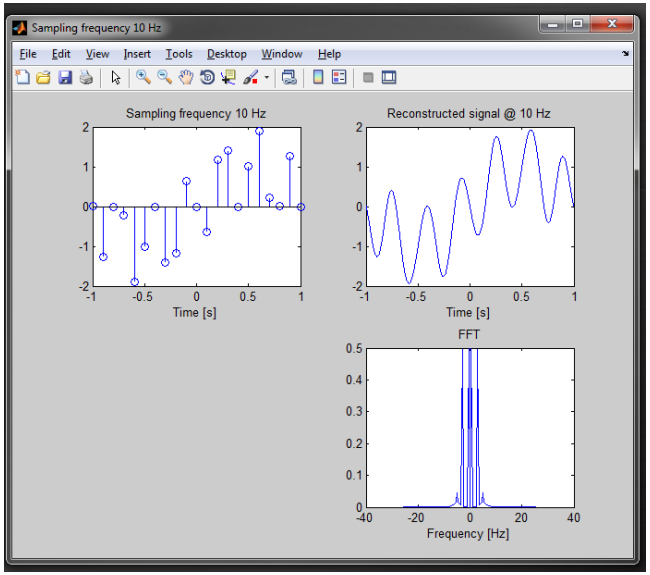
- $f(t) = \sum_i A_i \sin(2\pi f_i t)$
- frequencies
- amplitudes

- Not in this lab

- Sampling frequency

- Linear interpolation
- Whittaker-Shannon





Reconstruction: Linear vs. Wittaker-Shannon